

ANSWER TO 6.17

$$p^f = p^* = (1-\phi)p + \phi m$$

$$p^r = E p^* = (1-\phi)E p + \phi E m$$

$$p = q p^r + (1-q) p^f \quad \text{where } 0 < q < 1$$

$(m - E m)$  Error in expectation; surprise in AD

a) What's  $p^f$  given  $p^r, m$ .

$$p^f = (1-\phi)(q p^r + (1-q) p^f) + \phi m$$

Solve for  $p^f$ . Gives:

$$p^f = \frac{(1-\phi)q p^r + \phi m}{1 - (1-\phi)(1-q)}$$

Note  $1 - (1-\phi)(1-q) = \phi + (1-\phi)q$

$$\text{so } p^f = \frac{(1-\phi)q p^r + \phi m}{\phi + (1-\phi)q}$$

Look! Denominator is almost the same as coefficient on  $p^r$  in numerator.

Add to top  $\phi p^r - \phi p^r$

$$p^f = \frac{(1-\phi)q p^r + \phi m + \phi p^r - \phi p^r}{\phi + (1-\phi)q} = p^r + \frac{\phi}{\phi + (1-\phi)q} (m - p^r)$$

b) What's  $p^r$  given  $E_m$ ?

$$p^r = (1-\phi)E_p + \phi E_m = (1-\phi)E[qp^r + (1-q)p^f] + \phi E_m$$

$$= (1-\phi)E\left[qp^r + (1-q)p^r + (1-q)\frac{\phi}{\phi+(1-\phi)q}(m-p^r)\right] + \phi E_m$$

Use  $E p^r = p^r$  and solve for  $p^r$ :

$$p^r = (1-\phi)\left(p^r + (1-q)\frac{\phi}{\phi+(1-\phi)q}E_m - (1-q)\frac{\phi}{\phi+(1-\phi)q}p^r\right) + \phi E_m$$

$$\underbrace{\left(1 - (1-\phi) + \frac{(1-q)\phi}{\phi+(1-\phi)q}\right)}_{\phi} p^r = \left(\phi + \frac{(1-q)\phi}{\phi+(1-\phi)q}\right) E_m$$

$$p^r = E_m$$

c) Does  $\Delta E_m$  affect  $\gamma$ ? Does  $\Delta(m - E_m)$  affect  $\gamma$ ?Find  $p$  and  $\gamma$  as determined by  $m$  and  $E_m$ 

$$p = qp^r + (1-q)p^f = qp^r + (1-q)\left(p^r + \frac{\phi}{\phi+(1-\phi)q}(m-p^r)\right)$$

and gives  $p^r = E_m$

$$p = qE_m + (1-q)E_m + \frac{(1-q)\phi}{\phi+(1-\phi)q}(m - E_m)$$

$$= E_m + \frac{(1-q)\phi}{\phi+(1-\phi)q}(m - E_m)$$

6.16 (cont.)  
e) (cont.)

(3)

$$y = m - p \quad \text{so}$$

$$y = m - E_m - \frac{(1-q)\phi}{\phi + (1-\phi)q} (m - E_m)$$

$$= \frac{\phi + (1-\phi)q + (1-q)\phi}{\phi + (1-\phi)q} (m - E_m)$$

$$= \frac{q}{\phi + (1-\phi)q} (m - E_m)$$

See:  $\Delta E_m$  does not affect  $y$

$\Delta(m - E_m)$  does affect  $y$ .

Note: Small  $\phi$  makes  $\frac{\partial y}{\partial(m - E_m)}$  bigger

Small  $\phi$  means more "real rigidity":

$$P_i^* - p = \phi y$$

small  $\phi$  means output has little effect on desired relative price  
"Real rigidity"