

### ANSWER TO 7.3)

How do results of Taylor model depend on overlapping of price setting decisions? What if price adjustments are synchronized?

a) What is  $x_t = p_t = p_{t+1}$ ?

$$\text{Recall } p_t = E \left[ \sum_{t=0}^{\infty} \omega_t p_t^* \right]$$

$$\text{Here, } x_t = p_t = \frac{1}{2} p_t^* + \frac{1}{2} E_t p_{t+1}^*$$

$$\text{and } p_t^* = \phi m_t + (1-\phi) p \quad \text{hence}$$

$$x_t = \frac{1}{2} (\phi m_t + (1-\phi) p_t) + \frac{1}{2} (\phi E_t m_{t+1} + (1-\phi) E_t p_{t+1})$$

b) In terms of  $m_t$  and  $E_t m_{t+1}$  alone?

Everyone sets price equal to  $x_t$

$$\text{so } p_t = p_{t+1} = x_t$$

hence

$$x_t = \frac{1}{2} (\phi m_t + (1-\phi) x_t) + \frac{1}{2} (\phi E_t m_{t+1} + (1-\phi) x_t)$$

$$\Rightarrow x_t = \frac{1}{2} m_t + \frac{1}{2} E_t m_{t+1}$$

ANSWER TO 7.3) (cont.)

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c) What's  $y$  in each period, assuming  $m_{t+1} = m_t + e_{t+1}$  (i.i.d.)

$$p_t = p_{t+1} = \frac{1}{2} m_t + \frac{1}{2} m_t = m_t$$

hence  $E_t m_{t+1} = m_t$

$$y_t = m_t - p_t = m_t - m_t = 0$$

$$y_{t+1} = m_{t+1} - p_{t+1} = m_{t+1} - p_t = m_{t+1} - m_t = e_{t+1}$$

Note:  $\phi$  doesn't matter for effect of  $e$  on  $y$

$e_{t+1}$  won't affect  $y_{t+2}, y_{t+3}, \dots$

$$y_{t+2} = 0$$

$$y_{t+3} = e_{t+3} \leftarrow \begin{cases} \text{uncorrelated} \\ \text{with } e_t \end{cases}$$