

Guiding the Self-organization of Random Boolean Networks

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Self-organization

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- Pervasive concept, many definitions. Depends partly on observer.
- A notion: *A system described as self-organizing (SO) is one in which elements interact, achieving dynamically a global function or behavior* [Gershenson, 2007, p. 32].
- i.e. a *global* pattern is produced from *local* interactions.





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Spirit of the Wild
National Geographic magazine, September 2005



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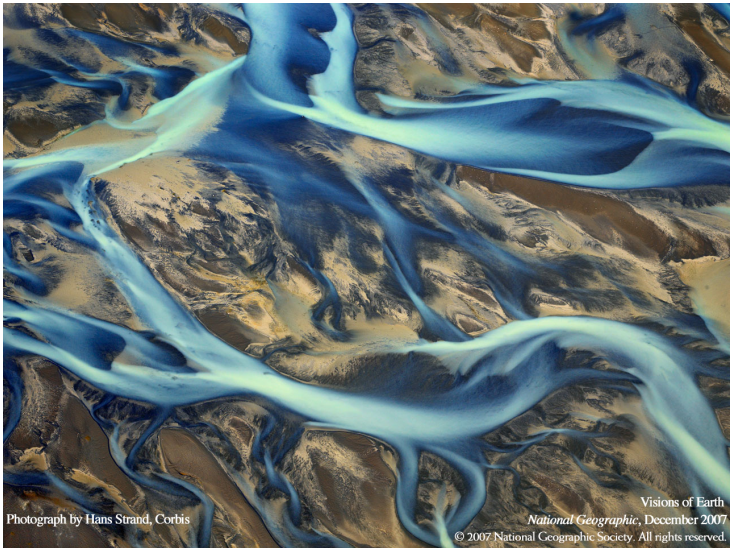
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Examples

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- a cell (molecules interact to produce life)
- a brain (neurons interact to produce cognition)
- a colony (insects interact to perform collective tasks)
- flocks, schools, herds (animals interact to coordinate collective behavior)
- a market (agents interact to define prices)
- traffic (vehicles interact to determine flow patterns)
- an ecosystem (species interact to achieve ecological homeostasis)
- a society (members interact to define social properties e.g. language, culture, fashion, esthetics, ethics, politics).



So... SO

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- Almost any system *can* be described as SO [Ashby, 1962].
- When is it *useful*? [Gershenson and Heylighen, 2003]
 - Properties at more than one scale.
 - Undefined or non-stationary spaces.
 - Interested in adaptation and robustness.
- Guided self-organization (GSO) [Prokopenko, 2009]: balance between design and self-organization.
- My GSO notion: *The steering of the self-organizing dynamics of a system towards a desired configuration.*
- GSO for understanding how natural systems achieve SO and for building artificial systems capable of SO.
- This talk: How can evolution guide the SO of genetic regulatory networks? How can we guide RBN self-organization towards a desired regime?



Random Boolean Networks (RBNs)

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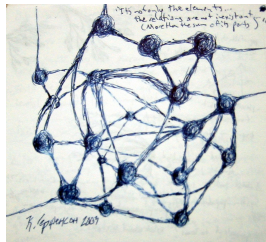
SO in RBNs

GSO in RBNs

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- RBNs originally models of genetic regulatory networks (GRNs) [Kauffman, 1969, Kauffman, 1993].
- Random connectivity and functionality + ensemble approach.
 - Useful when specific topology and functions cannot be defined.
- Possibility to explore possibilities of living and computational systems.
- Very general computational models.
 - Generalizations of Boolean CA.





Classic RBNs (several different flavors)

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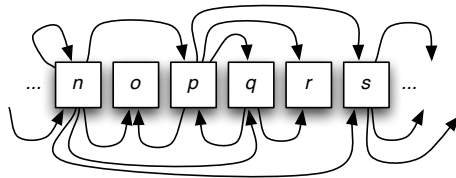
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- N Boolean nodes linked by K connections each.
- The state of a node at time $t + 1$ depends on the states of its K inputs at time t by means of a Boolean function.
- Connections and functions are chosen randomly when the RBN is generated and remain fixed during its temporal evolution.





E.g.

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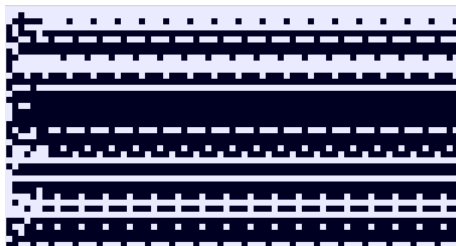
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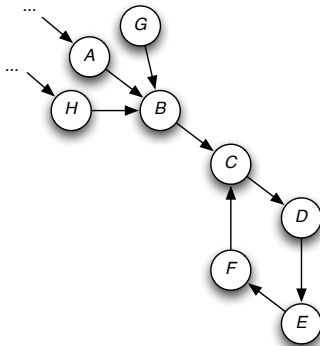
| $n(t)$ | $p(t)$ | $o(t+1)$ |
|--------|--------|----------|
| 0 | 0 | 1 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |





Dynamics on state space

- Attractors, basins.
- Dissipative systems, deterministic.
 - Only one successor, several or no predecessors.
- What is relationship between topological and state networks?





RBNs as self-organizing systems

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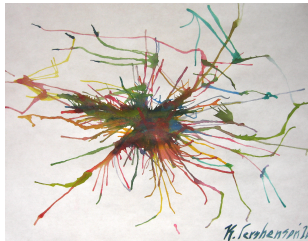
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- Dynamics “self-organize” towards attractors.
- Useful description to understand how the interactions between nodes (lower scale) affect the network dynamics and properties (higher scale).
- Complexity reduction.
 - $\sim 30,000$ genes in humans, only ~ 300 cell types (attractors).
- In which ways can the self-organization of random Boolean networks be guided?





Dynamical regimes I

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Conclusions

- Ordered, chaotic, and critical (near phase transition).
- *Ordered*: most nodes are static. Robust. Convergence of similar states.



- *Chaotic*: most nodes are changing. Fragile. Divergence of similar states.





Dynamical regimes II

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- *Critical*: balance: some nodes static, some changing. Changes spread locally. Maximization of information storage, coherent information transfer [Lizier et al., 2008], and Fisher information [Wang et al., 2010].



- Computation and life @ “edge of chaos” [Langton, 1990, Kauffman, 1993, Crutchfield, 1994, Kauffman, 2000].
 - Evidence from four kingdoms [Balleza et al., 2008].
 - Balance between robustness, information storage and variability, computation, exploration.
- How can SO of RBNs be guided towards criticality?



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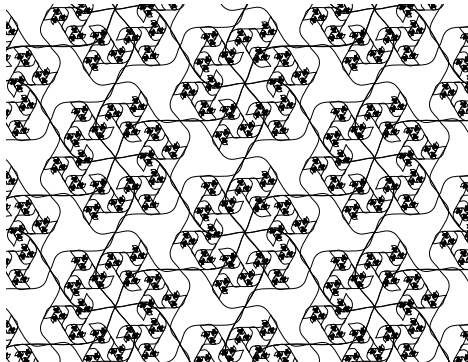
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The criticality of RBNs can depend on many different factors. These factors can be exploited—by engineers or by natural selection—to guide the self-organization of RBNs and related systems towards the critical regime.





p, K

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Probability p of having ones on the last column of lookup tables [Derrida and Pomeau, 1986]

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$$\langle K \rangle = \frac{1}{2p(1-p)}$$

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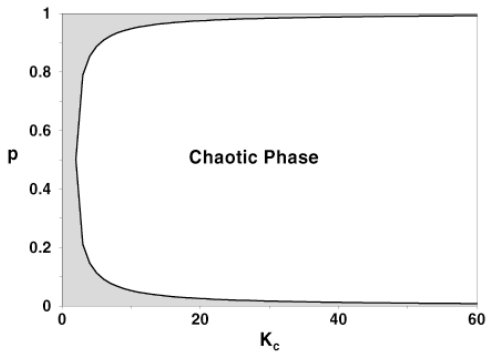
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Canalizing functions

- A canalizing function [Kauffman, 1969, Stauffer, 1987, Szejka and Drossel, 2007] is one in which at least one of the inputs has one value that is able to determine the value of the output of the function, regardless of the other inputs [Shmulevich and Kauffman, 2004].
- Non-canalizing inputs of canalizing functions are not relevant, i.e. fictitious. Altering them does not affect state space or dynamics of RBN.
- More canalization \Rightarrow higher K_c .

| $x(t)$ | $y(t)$ | $z(t+1)=\text{NOT } x$ |
|--------|--------|------------------------|
| 0 | 0 | 1 |
| 0 | 1 | 1 |
| 1 | 0 | 0 |
| 1 | 1 | 0 |

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Topology

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- Most RBN studies use homogeneous or normal topologies (uniform rank distributions): more and longer attractors, less correlation in expression patterns.
- Skewed topologies: less and shorter attractors, more correlations (entropy and mutual information) [Oosawa and Savageau, 2002].
- Balance achieved with scale-free topologies.
- RBNs with a scale-free topology expand the advantages of the critical regime into the ordered phase [Aldana, 2003]
 - Well-connected elements can lead to the propagation of changes
 - i.e. adaptability even when the average connectivity would imply a static regime.
 - Scale-free topology “expands the range of the critical regime”.



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- Prevalent property in natural systems [Callebaut and Rasskin-Gutman, 2005], desired in artificial ones [Simon, 1996].
- Modules offer a level of organization that promotes at the same time robustness and evolvability [Wagner, 2005b].
 - Damage within one module usually does not propagate through the whole system (robustness).
 - Useful changes can be exploited to find new configurations without affecting the functionality of other modules.
- Modules broaden the range of the critical regime in RBNs [Poblanno-Balp and Gershenson, 2010] towards the chaotic phase, since changes do not propagate as easily between modules.



Redundancy

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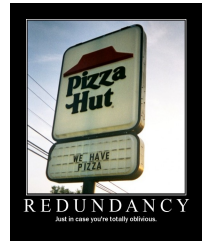
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- Redundancy consists of having more than one copy of an element type.
- Redundancy of nodes prevents mutations from propagating in RBNs [Gershenson et al., 2006]
- Can “smoothen” rough landscapes, increase neutrality, useful for robustness and evolvability.
- Can be combined with modularity.



Degeneracy

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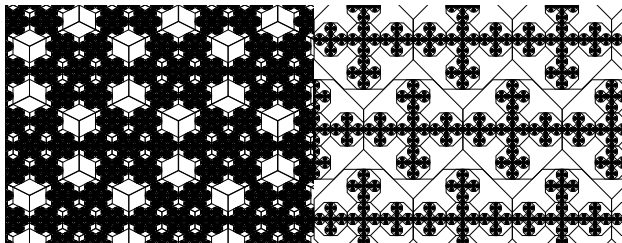
- Ability of elements that are structurally different to perform the same function [Edelman and Gally, 2001, Fernández and Solé, 2004]; or ability of elements to perform different functions [Whitacre and Bender, 2010].
- Also widespread in biological systems.
- Also promotor of robustness and evolvability, even more than redundancy [Wagner, 2005a, Wagner, 2005b].
- No RBN study yet, but can be speculated that degeneracy should promote critical dynamics.



Discussion

Two categories for GSO towards criticality: \sim functions and \sim topology

- Move the phase transition (p , K , or canalizing functions).
 - If too ordered, move $p \rightarrow 0.5$, increase K , and/or decrease canalization (if any).
 - If too chaotic, move $p \rightarrow 1$ or 0 , decrease K , and/or increase canalization.
- Broaden the critical regime (with a scale-free topology, modularity, redundancy, or degeneracy).
 - Promote one or more.



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Why criticality?

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- Balance: adaptability, evolvability, robustness.
- *Adaptability*: ability of a system to produce advantageous changes in response to a state of its environment [Gershenson, 2007].
- *Evolvability*: ability of random variations to sometimes produce improvement [Wagner and Altenberg, 1996]. Includes scalability. Particular type of adaptability.
- A system is *robust* if it continues to function in the face of perturbations [Wagner, 2005b, Jen, 2005]. Complements adaptability, interrelated.
- Topology and modularity → evolvability.
- Redundancy and degeneracy → robustness.



Open Questions

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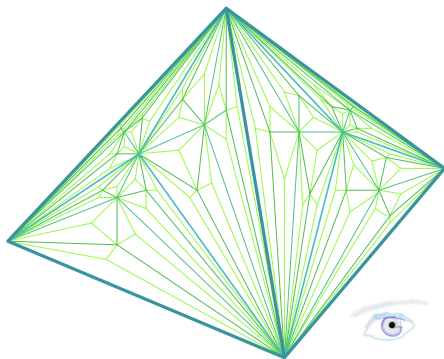
Conclusions

- What drove the evolution of criticality in GRNs?
[Balleza et al., 2008]
- Which methods have been exploited by natural selection?
- How are the different methods related?
 - How are scale-free and modular topologies related?
 - Is there an advantage of having both a scale-free topology and modularity over only one of them?
 - When is redundancy or degeneracy preferable?
 - What are the differences and advantages of critical RBNs produced with one or several of the presented methods?
 - How are different methods related to adaptability, evolvability, and robustness?
 - What is the proper balance between evolvability and robustness?



Conclusions

- Methods for GSO in RBNs reviewed.
- Useful for understanding natural and building artificial systems.
 - Can generalize some aspects from RBNs.
- Many open research avenues.



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Question time!

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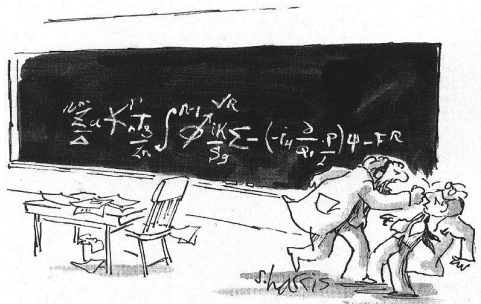
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"YOU WANT PROOF? I'LL GIVE YOU PROOF!"

More details:

Gershenson, C. (In Press). Guiding the Self-organization of Random Boolean Networks. *Theory in Biosciences*.

<http://arxiv.org/abs/1005.5733>



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